

Algebra II

SS 4

Solving Systems of Linear Equations in Three Variables

Equations in two variables define a line (1-dimension)

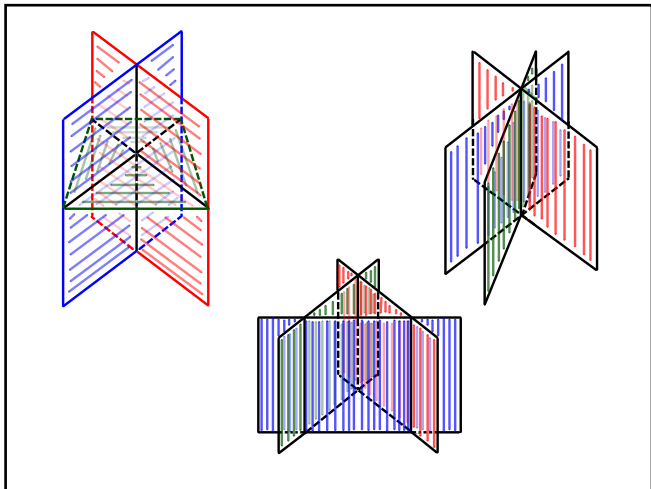
How many solutions are possible in the crossing of 2 lines? 3

- List them: 1) one point
 2) no points - parallel
 3) infinite solutions - one over the other

Equations in three variables define a plane (2-dimensions)

How many solutions are possible in the crossing of 3 planes?

- 1) infinite solutions
 2) one point 3) none



Solve each system. (pg 447)

$$\begin{aligned}
 1) \quad & x + y - 3z = 10 \\
 & y + z = 12 \\
 & z = -2
 \end{aligned}$$

$y + (-2) = 12$
 $y = 14$

$$\begin{aligned}
 x + (14) - 3(-2) &= 10 \\
 x + 20 &= 10 \\
 x &= -10
 \end{aligned}$$

$\{(-10, 14, -2)\}$

$$\begin{aligned}
 9) \quad & -2x + y + 3z = 10 \\
 & x - 2y + z = 10 \\
 & -4x + 3y + 2z = 5
 \end{aligned}$$

$4x + 2y + 6z = 20$
 $-4x + 3y + 2z = 5$
 $\hline 5y + 8z = 25$

$2x + y + 3z = 10$
 $-2x + 4y - 2z = -20$
 $\hline 5y + z = -10$

$-5y - z = 10$
 $5y + 8z = 25$
 $\hline 7z = 35$
 $z = 5$

$x - 2(-3) + (5) = 10$
 $x + 11 = 10$
 $x = -1$

$5y + (5) = -10$
 $5y = -15$
 $y = -3$

$\{(-1, -3, 5)\}$

pg 447
1-12 all